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Object :-

By use of C-program given above, find the root of the equation -

$$x^4 - x - 10 = 0$$

by Bisection method

Soln We know that if the function $f(x)$ is, continuous between two real values x_0 , x_1 and $f(x_0)$ and $f(x_1)$ are of opposite signs, i.e., $f(x)$

$f(x) < 0$ then there must be a root of $f(x) = 0$ between x_0 and x_1 , let $f(x)$ be negative and $f(x)$ be positive, ~~then~~

Now divide x , is the real root root of $f(x) = 0$
But if $f(x_1) \neq 0$ then the real root of $f(x) = 0$

will lie either in $[x_0, x_1]$ or $[x_1, x_1]$.
If $f(x)$ is positive, then the root will lie in $[x_1, x_1]$.

Since $f(x_2) < 0$ and if $f(x_2)$ is negative the root lies in $[x_2, x_2]$.

Since $f(x_2) \cdot f(x_2)$.

Teacher's Signature _____

Similarly, the interval in which the origin is located is further divided into two equal parts until the value of the origin is known to the desired accuracy.

The C-program to find the roots of the equation $f(x) = 0$ by bisection method.

```
/* BISECTION METHOD */
```

```
# include <stdio.h>
```

```
# include <conio.h>
```

```
# include <math.h>
```

```
# define f(x) x*x*x - 2.0*x - 5.0 /*  
    write given equation */
```

```
void main () ,
```

```
float x, x0, x1, x2, y1, y2, e,
```

```
clrscr ();
```

```
printf ("Input two initial starting roots\n");  
scanf ("%f%f", x0, x1);
```

Teacher's Signature _____


```
Print ("Input the tolerance value \n");  
scanf ("%f", &e);
```

```
y0 = f(x0);
```

```
y1 = f(x1);
```

```
if (y0*y1 > 0.0)
```

```
{
```

```
Print ("Initial are unsuitable \n")
```

```
}
```

```
else
```

```
{
```

```
while (fabs (x1-x0)/x1) > e)
```

```
{
```

```
x2 = (x0+x1)/2;
```

```
y2 = f(x2);
```

```
if (y0*y2 > 0)
```

```
x0 = x2;
```

```
else
```

```
x1 = x2;
```

Teacher's Signature _____

Object :-

Write a C-program for finding the root of the equation -

$$x^3 - 2x - 5 = 0$$

by using Bisection method in the interval $[2, 3]$ correct up to three-decimal places.

Solⁿ :-

We know that if the function $f(x)$ is continuous between two real values x_0 , x and $f(x_0)$ and $f(x_1)$ are of opposite signs, i.e., $f(x_0) > 0$, $f(x_1) < 0$, then there must be a root of $f(x) = 0$ between x_0 and x_1 . Let $f(x_0)$ be negative and $f(x_1)$ be positive.

Now divide the interval $[x_0, x_1]$ into two equal parts by a x_2 point lying between them.

If $f(x_2) = 0$, then x_2 is the real root of $f(x) = 0$. But if $f(x_2) \neq 0$ then x_2 is the root of $f(x) = 0$.

will lie either in $[x_0, x_2]$ or $[x_2, x_1]$. If $f(x_2)$ is positive, then the root will lie in $[x_2, x_1]$. Since $f(x_2) > 0$ and if $f(x_1)$ is negative, then the root will lie in $[x_2, x_1]$.

Teacher's Signature _____

}

Print ("Solution converges to a root\n");
Print ("In Root of the given equation is 1.
8.3 f⁴ x 2");

}

getch ();

}

Input :-

Input two initial starting roots

1.2

Input the tolerance value

0.0001

Output :-

Solution converges to a roots

Roots of the given equation

is = 1.856

Teacher's Signature _____

negative the root lies in $[x_1, x_2]$;
Since $f(x_1) \cdot f(x_2)$

Similarly,

The interval in which the origin
the origin is located is further divided into
two equal parts until the value of the
origin is known to the desired accuracy.

The C-program to find the roots of the
equation $f(x) = 0$ by bisection method.

```
/* BISECTION METHOD */
```

```
#include <stdio.h>
```

```
#include <conio.h>
```

```
#include <math.h>
```

```
#define f(x) x*x*x - 2.0*x + 5.0 /*  
write given equation */
```

```
void main ( )
```

```
{
```

```
float x, x0, x1, x2, y0, y2, e;
```

```
clrscr ( );
```

Teacher's Signature _____


```
Print ("Input two initial starting roots\n");  
scanf ("%f %f", x0, x1);
```

```
Print ("Input the tolerance value\n");  
scanf ("%f", e);
```

```
y0 = f(x0);  
y1 = f(x1);
```

```
if (y0 * y1 > 0.0 >
```

```
{
```

```
Print ("Initial values are unsuitable\n");
```

```
{
```

```
else
```

```
{
```

```
while ((fabs(x1 - x0) / x1) > e)
```

```
{
```

```
x2 = (x0 + x1) / 2;
```

```
y2 = f(x2);
```

```
if (y0 * y2 > 0)
```

```
x0 = x2;
```

Teacher's Signature _____

else

$$x_1 = x_2;$$

{

Print ("Solution converges to a root in");
Print ("In Root of the given equation
is $8.3 f'' x_2$ ");

{

getch ();

{

Input :-

Input Two Initial Starting roots

2, 3

Input The Tolerance Value

0.0001

Output :-

Solution converge to a root

Root of the given equation
is = 2.095

Teacher's Signature _____

object :-

By using C-program, find a real root of the equation —

$$x^2 + x - 1 = 0$$

Which lies in $[0, 1]$ correct upto three places of decimal by method of false position.

solⁿ :-

The iteration formula for the false position method.

(Regula falsi method) is as follows ; "

$$x_{n+1} = \frac{x_{n-1} f(x_n) - x_n f(x_{n-1})}{f(x_n) - f(x_{n-1})}$$

Where, $n = 1, 2, 3, \dots$

C - program

/* Root of an Equation by Regula - falsi method */

include < stdio.h >

include < conio.h >

include < math.h >

define f(x) $x^2 + x - 1$ write given equation*

void main ()

Teacher's Signature


```
{  
    float x0, x1, x2, f0, f1, f2, e;  
    int max_iteration
```

```
clear ( );
```

```
    Print ("Input Two Initial Roots, maximum  
           iteration and tolerance value:");
```

```
    scanf ("%f %f %d %f", &x0, &x1,  
           &max_iteration, &e);
```

```
    f1 = f(x1)
```

```
    if (f0 * f1 > 0.0)
```

```
{
```

```
    Print ("Initial roots are unsuitable\n");
```

```
}
```

```
    else
```

```
{
```

```
        for (i = 1; i < max_iteration; i++)
```

```
{
```

```
    x2 = (x0 * f1 - x1 * f0) / (f1 - f0);
```

```
    f2 = f(x2)
```

```
    if (fabs(f2) < e)
```

Teacher's Signature _____

{

Print ("Solution is converge in");

Print ("Root of the given equation is
= %.8.4%. /h" x2);

max_iteration = i;

}

else

{

if ($f_2 * f_0 < 0$)

{

$x_1 = x_2$;

$f_1 = f_2$;

}

else

{

$x_0 = x_2$;

$f_0 = f_2$;

}

}

}

Teacher's Signature _____

}

getch ();

{

Input :-

Input Two Initial Roots, maximum iterations and tolerance value;

0

1

1.0

0.0001

Output :-

Solution is converge

Roots of the given equation
is $= 0.618$

Teacher's Signature _____

Object :-

By using above C-program find the real root between 1.5 and 1.6 to four decimal of the equation -

$$x^6 - x^4 - x^3 - 3 = 0$$

Position method.

by false

Soln :-

The iteration formula for the false position method (Regula Falsi method) is as follows:

$$x_{n+1} = \frac{x_{n-1} f(x_n) - x_n f(x_{n-1})}{f(x_n) - f(x_{n-1})}$$

Where $n = 1, 2, 3, \dots$

C-program

```
/* Root of an equation by Regula - falsi method */
```

```
#include <stdio.h>
```

```
#include <conio.h>
```

```
#include <math.h>
```

```
#define f(x) x*x + x - 1 /* write  
given equation */
```

Teacher's Signature


```
void main ( ) ;
```

```
{
```

```
float x0, x1, x2, i0, i1, i2, e;
```

```
int max_iteration
```

```
close ( ) ;
```

```
Print ("Input Two Initial Roots, maximum  
iteration and tolerance value:");
```

```
scanf ("%f %f %d %f", &x0, &x1,  
&max_iteration, &e);
```

```
f0 = f(x0);
```

```
f1 = f(x1);
```

```
if (f0 * f1 > 0.0)
```

```
{
```

```
Print f ("Initial roots are unsuitable\n");
```

```
}
```

```
else
```

```
{
```

```
for (i=1; i <= max_iteration; i++);
```

Teacher's Signature _____

{

$$x_2 = (x_0 * f_1 - x_1 * f_0) / (f_1 - f_0);$$

$$f_2 = f(x_2)$$

if (fabs(f2) < e)

{

Print f ("1 solution is conver ln")

Print ("1 Root of the given equation
is = 1.84 1. ln", x2);

max_iteration = i;

{

if (f2 * f0 < 0)

{

$$x_1 = x_2;$$

$$f_1 = f_2;$$

{

else

{

$$x_0 = x_2;$$

Teacher's Signature _____

$f_0 = f_2;$

}

}

}

}

getch ();

}

Input :-

Input Two Initial Roots, maximum iterations and tolerance Value.

1.5 1.6 10 0.00001

Output :-

Solution in converge

Root of the given equation is = 1.5018.

Teacher's Signature _____

object :-

Write a C-program by using Newton-Raphson method, find the root of the equation -

$$x^3 - 3x - 5 = 0$$

correct to four decimal places line in $[2, 3]$

solⁿ :-

The iterative formula for Newton-Raphson method.

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

Where, $f'(x_n)$ is the first derivative of $f(x_n)$ with respect to x_n .

C-program.

```
/* Newton-Raphson method */
```

```
#include <stdio.h>
```

```
#include <conio.h>
```

```
#include <math.h>
```

Teacher's Signature _____


```
#define f(x) x*x*x-3*x-5 /* Given  
equation */
```

```
#define df(x) 3*x*x-3 /* Differential  
of equation */
```

```
void main ( )
```

```
{
```

```
long float x0, x1, f0, f1, y1, x, e;  
long int i, maxiter;
```

```
clrscr ( );
```

```
Print ("Input initial root, max. iterations  
and tolerance value: \n");
```

```
scanf ("%lf", & x0  
        & maxiter, & e);
```

```
for (i=1; i <= maxiter; i++)
```

```
{
```

```
    f0 = f(x0);
```

```
    f1 = df(x0);
```

```
    x1 = x0 - (f0/f1);
```

Teacher's Signature _____


```
if ((f abs(x1 - x0) / x1 < e)
{
    Print f ("Solution converges to a
              roots\n");
    Print f ("Number of Iteration
              = %d\n", i);
    Print f ("Root of the given equation
              is = %.8f\n", x1);
    i = maxiter
}
else
{
    x0 = x1;
}
getch();
}
```


Input :-

Input Initial root, max. iterations
and tolerance Value.

2 10 0.00001

output :-

Solution Converges to a root

Number of Iterations = 4

Root of the given equation
is = 2.2790

Teacher's Signature _____

object :-

By using above C-program, find the root of the equation -

$$x^3 + x^2 - 1 = 0$$

correct to four places of decimal by Newton - Raphson method.

Soln :-

The iterative formula for Newton-Raphson method.

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

Where,

$f'(x_n)$ is the first derivative of $f(x_n)$ with respect to x_n .

C-program.

```
/* Newton - Raphson method */
```

```
#include <stdio.h>
```

```
#include <conio.h>
```

```
#include <math.h>
```

Teacher's Signature


```
# define f(x) x*x*x-3*x-5 /* Given  
equation */
```

```
# define df(x) 3*x*x-3 /* Differential  
of equation */
```

```
void main ( )
```

```
{
```

```
long float x0, x1, f0, f1, y1, x, e;  
long int i, maxiter;
```

```
clrscr ( ) ;
```

```
Print { " | Input Initial x0, max.  
iterations and tolerance value: | " };
```

```
scanf ("%f %d %f", &x0, &maxiter,  
&e);
```

```
for (i=1; i <= maxiter, i++);
```

```
{
```

```
    f0 = f(x0);
```

```
    f1 = df(x0);
```

```
    x1 = x0 - (f0 / f1);
```

Teacher's Signature _____


```
if (if abs (x1 - x0) / x1) < e)
```

```
{
```

```
Print f ("Solution Converges to a  
roots 1n");
```

```
Print f ("Number of Iteration  
= %d 1n", i);
```

```
Print f ("Root of the given equation  
is = %f / f", x1);
```

```
i = maxiter;
```

```
}
```

```
else
```

```
{
```

```
x0 = x1
```

```
}
```

```
}
```

```
getch ();
```

```
}
```

Teacher's Signature _____

Input :-

Input Initial root, max. iterations
and tolerance value:

0.5

10

0.00001

Output :-

Solution converges to a root

Number of Iterations = 5

Root of the given equation
is = 0.7548.

Teacher's Signature _____

object :-

By use of c-program given above the following system of equation by Gauss-elimination method:

$$8x_1 + 4x_2 + 2x_3 = 24$$

$$4x_1 + 10x_2 + 5x_3 + 4x_4 = 32$$

$$2x_1 + 5x_2 + 6.5x_3 + 4x_4 = 26$$

$$4x_2 + 4x_3 + 9x_4 = 21$$

Soln :-Gauss Elimination method :-

under this method the coefficient matrix with in the augmented matrix of the given system of linear algebraic equation is converted into an upper triangular matrix using elementary row operation.

There after, the values of the unknown variables are determined using the back-substitution method.

[computer Application with c-program]

/* c-program for Gauss - Elimination

#include <stdio.h>

#include <conio.h>

Teacher's Signature _____


```
void main ( )  
{  
    int i, j, k, n;  
    float a [10] [10], x [10], sum, temp;  
    printf ("Enter Number of system of  
            equations |n|n");  
    scanf ("%d", &n);  
    printf ("Number of equations  
            are = %d |n", n);  
    clrscr ( );  
    printf ("Enter coefficients of linear  
            equations /  
            coefficients of augmented matrix  
            |n|n");  
    for (i=0; i<n; i++)  
    {  
        for (j=0; j<n; j++)  
        {
```

Teacher's Signature _____


```
for (j = 0; j < n + 1; j++)  
    scanf ("%f", &a[i][j]);  
}  
/* Calculate upper triangular matrix */  
for (i = 1; i < n + 1; i++)  
{  
    temp = 0.0;  
    for (j = i + 1; j <= n; j++)  
    {  
        temp = a[i][j] / a[i][i];  
        for (k = i; k <= n + 1; k++)  
            a[i][k] = a[j][k] - (temp * a[j][k]);  
    }  
}  
/* Print upper triangular matrix */
```

Teacher's Signature _____


```
Print ("In upper triangular matrix is : \n \n");
```

```
for (i = 1; i <= n; i++)
```

```
{
```

```
    for (j = 1; j <= n + 1; j++)
```

```
    {
```

```
        for (j = 1; j <= n + 1; j++)
```

```
            Print f ("%B.2 f", a[i][i]);
```

```
            Print f ("\n");
```

```
    }
```

```
/* evaluate unknowns by back substitution */
```

```
x[n] = a[n][n+1] / a[n][n];
```

```
for (i = n - 1; i >= 1; i--)
```

```
{
```

```
    sum = 0.0;
```

```
    for (i + 1; j <= n; j++)
```

```
    {
```

Teacher's Signature _____


```
Sum = Sum + (a[i][j] * x[j]);  
}
```

```
x[i] = a[i][n+1] - Sum / a[i][i]  
}
```

```
Print f("\n | Solution of the equation is\n\n");
```

```
for (i = 1; i <= n; i++)
```

```
Print f("x [%d] = %.8f\n", i, x[i]);
```

```
getch ( );
```

```
}
```

Input:-

Enter Number of system of equations.

Number of Equations are = 4

Teacher's Signature _____

Enter Coefficients of linear equations / coefficients of augmented matrix:

$$\begin{bmatrix} 8 & 4 & 2 & 0 & 24 \\ 4 & 10 & 5 & 4 & 32 \\ 2 & 5 & 6.5 & 4 & 26 \\ 0 & 4 & 4 & 9 & 21 \end{bmatrix}$$

output :-

Upper Triangular matrix is:

$$\begin{bmatrix} 8.00 & 4.00 & 2.00 & 0.00 & 24.00 \\ 0.00 & 8.00 & 4.00 & 4.00 & 20.00 \\ 0.00 & 0.00 & 4.00 & 2.00 & 10.00 \\ 0.00 & 0.00 & 0.00 & 6.00 & 6.00 \end{bmatrix}$$

Solution of the equations is:

$$x[1] = 2.00$$

$$x[2] = 1.00$$

$$x[3] = 2.00$$

$$x[4] = 1.00$$

Teacher's Signature _____

object :-

Write a C-program for the following system of linear equations by using Gauss - Elimination method.

$$2x - 8y - 2z = 14$$

$$x + 6y - z = 13$$

$$2x - y + 2z = 5$$

Soln :-

Gauss - Elimination method :-

Under this method the coefficient matrix with in the augmented matrix of the given system of linear algebraic equations is converted into an upper triangular matrix using elementary row operations.

Thereafter, the values of the unknown variables are determined using the back-substitution method.

[Computer Applications with C-program]

/* C-program for Gauss - Elimination method

#include <stdio.h>

#include <conio.h>

Teacher's Signature _____


```
void main ( )  
{  
    int i, j, k, n;  
    float a[10][10], x[10], sum, temp;  
    printf ("Enter Number of system of  
            equations in n");  
    scanf ("%d", &n);  
    printf ("Number of Equations are = %d\n", n);  
    clrscr ( );  
    printf ("Enter coefficients of linear  
            equations/  
            coefficient of augmented matrix in n");  
    for (i=0, i<n; i++)  
    {  
        for (j=0, j<n+1; j++)  
            scanf ("%f", &a[i][j]);  
    }
```

Teacher's Signature _____


```
/* calculate upper triangular matrix */
```

```
for (i = 1; i < n - 1; i++)
```

```
{
```

```
    temp = 0.0;
```

```
    for (j = i + 1; j <= n; j++)
```

```
    {
```

```
        temp = a[i][i] / a[i][j];
```

```
        for (k = i; k <= n + 1; k++)
```

```
            a[i][k] = a[j][k] - temp * a[i]
```

```
        }
```

```
    }
```

```
/* Print upper triangular matrix */
```

```
Print f("In upper Triangular matrix  
is : In In");
```

```
for (i = 1; i <= n; i++)
```

Teacher's Signature _____

{

for (j = 1; j ≤ n + 1; j++)

Print f ("%f B.2 f", a[i][j]);

Print ("ln");

}

/* evaluate unknowns by back substitution */

 $x[n] = a[n][n+1] / a[n][n];$

for (i = n - 1; i ≥ 1; ...)

{

sum = 0.0;

for (j = i + 1; j ≤ n; j++)

{

sum = sum + (a[i][j] * x[j]);

}

 $x[i] = a[i][n+1] / \text{sum}$

}

Teacher's Signature _____


```
Print f ("n| Solution of the equation is : |n|n");
```

```
for (i=1 <= n; i++)
```

```
Print ("x [%d] = %.8.3 f\n", i, x[i]);
```

```
    getch ( );
```

```
}
```

Input:-

Enter Number of system of equations.

Number of equations are = 3

Enter coefficients of linear equations /
coefficients of augmented matrix:

$$\begin{bmatrix} 2 & 8 & 2 & 14 \\ 2 & 6 & -1 & 13 \\ 2 & -1 & 2 & 5 \end{bmatrix}$$

Teacher's Signature _____

output :-

Upper Triangular matrix is :

$$\begin{bmatrix} 2.00 & 8.00 & 2.00 & 14.00 \\ 0.00 & 2.00 & -2.00 & 6.00 \\ 0.00 & 0.00 & -9.00 & 18.00 \end{bmatrix}$$

Solution of the equation is :

$$x[1] = 5.00$$

$$x[2] = 1.00$$

$$x[3] = -2.00$$

Teacher's Signature _____